1 2 Part 2: "Surfer Speed vs. Wave Speed and Peel Angle" 3 4 by Larry Goddard 5 August 14, 2010 6 7 8 Part 1 was a tutorial on the Physics of Motion and the relationship between Work and Energy. Therefore, 9 Part 1 was written to lay the groundwork for understanding Part 2. Maybe boring for some readers, mind-10 numbing for others, but necessary for most people, I think. If you digested the material covered in Part 1, then you are ready for Part 2. Thanks for your patience! 11 12 13 Part 2 is where 'the rubber hits the road', and we find answers to questions about "Maximum Surfer 14 Speed on a Wave." 15 Part 1 also tried to answer the question: "How fast IS the surfer going on a wave?" 16 17 Part 2 will try to answer the question: "How fast CAN a surfer go on a wave?" 18 19 A surfer on a wave is constantly managing his Energy budget, trading the Potential Energy that he 20 obtained by going up high on the wave, for more Kinetic Energy and therefore higher speed when he 21 needs it, down lower on the wave. 22 23 A roller coaster does exactly the same thing. The cars and riders are mechanically lifted to the top of the 24 first, and highest, rise of the tracks. The amount of Potential Energy obtained at the top is exactly identical 25 to the amount of Work that was performed in lifting the combined Weight of the cars and riders up to that Height above their starting point at ground level. 26 27 28 Then, the cars are released and are free to roll downhill, gaining Speed and Kinetic Energy all the way 29 down to the bottom. If there were no drag or friction, the Kinetic Energy at the bottom would be identical 30 to the Potential Energy they started out with at the top. KE = PE. 31 32 Because of the total drag (due to friction and air drag) though, their total Energy budget is slowly eroding, 33 and so each succeeding hill is less high, until finally, the cars are brought in to the loading station and 34 brought to a stop with braking action. 35 36 When you are sitting in the surf line-up, waiting for the next set, you are starting out in a position, (on 37 average), at Sea Level, where your Potential Energy and Kinetic Energy are both zero. 38 39 Then, as the wave you want approaches, it starts lifting you and your board up towards the top of the 40 wave. If it lifts you all the way up to the top of wave, just as you are about to catch it by paddling fast enough for you to start sliding downhill and then match the wave speed, you have now gained Energy of 41 42 Position, that is, "Potential Energy", AND, by matching the wave's speed, you have now ALSO gained Energy of Motion, that is, "Kinetic Energy". This combination of PE and KE is your Total Energy Budget. 43 44 45 If you don't paddle for the wave, then the only Energy you have at the top of the wave is PE. But if you DO paddle for the wave, then when you match the wave speed and can stand up, you have gained the 46 energy of motion due to the Wave Speed. I'll call that "KEwave". Just remember: that's YOUR Kinetic 47 48 Energy when moving at the Wave Speed.

So, at the top of the wave, just as you match the wave speed, but just BEFORE you make the drop, we can say that: Total Energy, or KEtotal = PE + KEwave Remember: PE is the WORK that the wave performs by lifting you and your board up to the top of the wave, that is, PE = WORK = Weight times Height = W\*H, where W is the total Weight lifted, and H is the Height lifted to, i.e., the Wave Height. When you make the drop, but just before you turn, you trade your Potential Energy at the top of the wave for additional Kinetic Energy at the bottom of your drop. At that point, you are moving faster then the Wave Speed. If you could make it all the way to the Bottom of the wave before you turn, you would have KE = PE. Let's call that Kinetic Energy obtained from making the drop, "KEdrop." Now, our Total Energy, KEtotal = KEwave + KEdrop I'm going to relabel the Total Energy as the "Surfer Energy", since that's his Total Energy Budget, and is what gives him the ability to go fast across the wave, or race fast sections, or just climb back up high and bang off the lip, or be set up for the next maneuver. So, now we have: KEsurfer = KEwave + KEdrop The formula for Kinetic Energy is  $(1/2)^*(W/g)^*V^2$ , or KE =  $(W/2g)^*V^2$ Note that KE varies with the SQUARE of the Velocity of the moving body. So. For a surfer moving at full trim speed across a wave, KEsurfer =  $(W/2g)^{*}(Vsurfer)^{2}$ For a surfer at the top of a wave, moving at Wave Speed, KEwave = (W/2g)\*(Vwave)^2 For a surfer who just dropped in, about to make his turn, KEdrop =  $PE = W^*H$ So, if KEsurfer = KEwave + KEdrop, Then, (W/2g)\*(Vsurfer)^2 = (W/2g)\*(Vwave)^2 + W\*H Solving for (Vsurfer)^2, we get:  $(Vsurfer)^{2} = [(W/2g)^{*}(Vwave)^{2} + W^{*}H] / (W/2g)$ Or,  $(Vsurfer)^{2} = [(W/2g)^{*}(Vwave)^{2} + W^{*}H]^{*} (2g)/W$ Cancelling the W and the 2g terms, we get:  $(Vsurfer)^2 = [(Vwave)^2 + 2gH]$ Remember that, in a right triangle, c squared = a squared + b squared, Or,  $c^2 = a^2 + b^2$ 

101 So. 102 In the above result, it looks like we have the SQUARE of the hypotenuse of a right triangle, represented 103 by the SQUARE of the surfer's speed "Vsurfer", with the SQUARE of one side of the triangle represented by the SQUARE of the Wave Speed, "Vwave"; and the SQUARE of the other side of the triangle 104 105 represented by the SQUARE of the speed of the curl as measured at right angles to the wave speed, given by its equivalent squared value, "2gH". 106 107 108 So, we see that  $(Vcurl)^2 = 2gH$ 109 Now, let's rewrite this solution for Surfer Speed, using the formula for Wave Speed that was given in Part 110 111 1 of this document, where: 112 113 Vwave = SQRT  $(q^*d)$ , 114 Or. 115  $Vwave = (g^*d)^{0.5}$ 116 117 Then,  $(Vwave)^2 = g^*d$ , 118 119 But, if we use a Breaker Depth Index value of 1.28, then: d / Hb = 1.28, 120 So, d = 1.28 times Hb, or: d = 1.28\*Hb where "Hb" is the Breaking Wave Height. 121 122 Now, we have:  $(Vwave)^2 = 1.28^{\circ}g^{\circ}Hb$ 123 124 Substituting these in the Surfer Speed formula, we know have: 125 126  $(Vsurfer)^2 = (Vwave)^2 + (Vcurl)^2$ 127 128 So,, 129  $(Vsurfer)^{2} = 1.28 g^{Hb} + 2 g^{Hb}$ 130  $(Vsurfer)^{2} = (1.28+2)^{*}(g^{*}Hb)$ 131  $(Vsurfer)^{2} = 3.28^{*}(g^{*}Hb)$ 132 133 So, now we have the formula for Maximum Surfer Speed: Vsurfer = SQRT(3.28\*g\*Hb)134 135 136 But look! We can compare this Maximum Surfer Speed to the Wave Speed: 137 The ratio of  $(Vsurfer)^2 / (Vwave)^2 = (3.28*g*Hb) / (1.28*g*Hb)$ 138 = (3.28/1.28)139 = 2.5625 140 141 142 So, Vsurfer / Vwave = SQRT (2.5625) = 1.600781059 143 144 It looks like the fastest you could go on any wave is about 1.6 times as fast as the Wave Speed! 145 Remember that in Part 1 we found that Cos B = (Vwave / Vsurfer)? 146 147 That is just the reciprocal of the above ratio of Surfer Speed to Wave Speed. 148 So. 149 Cos B = SQRT (1.28/3.28) = SQRT(0.390243902) = 0.624695048 150 151 Then, 152 The Break Angle B is the ANGLE whose Cosine = 0.624695048),

153 Or. B = ArcCosine (0.624695048)154 155 B = 51.34019175 Degrees 156 157 This is for a surfer cruising in a straight line across a wave at his highest trim speed. If he stays up high on the wave where the highest speed is possible, he would be able to dive lower to gain some additional 158 speed going through a short fast section up ahead, and maybe be able to make it out the other side. 159 160 Generalizing in regards to the Breaker Depth Index, BDI, it would appear that the highest surfer speed 161 162 relative to wave speed is proportional to the square root of the ratio 163 (BDI +2) / BDI) 164 165 So. 166 Max Surfer Speed / Wave Speed = SQRT[(BDI +2) / BDI] 167 And, 168 Maximum Makeable Break or Peel Angle = ArcCosine [BDI / (BDI+2)] 169 170 171 So far, we've only determined the RATIOS of speeds involved in surfing a wave. Let's see what kind of 172 ACTUAL SPEEDS are therefore possible on waves of given heights. 173 174 For Makaha Point Break, where the 25 ft waves peel off pretty fast on WNW swells, the Acceleration of Gravity at the Latitude of the Point Line-up is about 32.110407 ft/sec^2. 175 176 177 I'll use the rounded off value of 32.11 f/s^2, because I got the Latitude from Google Earth aerial photos and had to interpolate to estimate the position of the reef block where the line-up is located. I am very 178 179 familiar with that reef, because I snorkelled out there often for 15 years. It should be accurate to within 10 180 ft or 3 meters. 181 182 If the water depth where 25 ft waves break is 1.28 times the breaking wave height, Hb, then the depth d = 183 1.28\*25 = 32 ft. 184 185 Then, the Wave Speed in 32 ft of water,  $Vwave = SQRT(q^*d) = SQRT(32.11^* 32)$ 186 So. Vwave,fps = 32.05495282 fps 187 188 And, 189 Vwave,mph = (15/22)\*Vwave,fps = 21.85564965 MPH 190 If Maximum Makeable Break Angle = 51.34019175 degrees, 191 Then, Maximum Surfer Speed = SQRT(3.28/1.28) times Wave Speed =1.600781059x Vwave 192 So. 193 Max Vsurfer = 1.600781059 x Vwave = 51.31296133 ft/sec = 34.98610999 MPH 194 195 196 If the ride is 400 vards = 1200 feet, the duration time of the ride = 1200/Vsurfer So, T,ride = 1200ft / 51.31296133fps = 23.38590424 seconds. 197 198 199 Buzzy Trent did it in 24 seconds... I never saw anybody do it in 23 seconds. 200 201 For more Northern Latitudes like, say that of San Francisco, where g= 9.8m/s^2, 202 Or, g = 32.155223097 f/s^2, 203 Then, 204 Vwave = 32.07602518 ft/sec, so Max Vsurfer = 51.34669356 fps.

205	Then, Maximum Surfer Speed = 35.00910925 MPH.
206 207	Thus, it looks like Vmax for 25 ft waves is around 35 MPH.
208	
209 210	Now, for a general formula for calculating Surfer Speed, given Wave Height:
	Maximum Stuffer Speed seems to be preparticulate the SOUMER BOOT of the Breaking Ways Usight
211	Maximum Surfer Speed seems to be proportional to the SQUARE ROOT of the Breaking Wave Height,
212	so, at the latitude of Makaha down to the South Shore (Ala Moana Bowls, and Waikiki in general), where
213	g = 32.11 f/s^2, the Maximum Surfer Speed for a 1 foot wave scales down to about 1/5th as fast as for
214	that of a 25 ft wave, or about 1/5th of 35 MPH. Therefore, we could use a general formula for Hawaiian
215	waters up to Northern California surf spots, that says:
216	
217	Maximum Surfer Speed, MPH = 7* SQUARE ROOT of (Hb,ft)
218	Or,
219	Maximum Surfer Speed, fps = 10.266666666668 SQUARE ROOT of (Hb,ft)
220	
221	Note:
222	The exact value of "g" required to produce the above values of 7 MPH EXACTLY for my Maximum Surfer
223	Speed, if we use a Breaker Depth Index of exactly 1.28, is 32.1355013550,etc. ft/sec^2, where the
224	"13550" is a repeating decimal.
225	
226	So, the exact decimal fraction is 13550/99999, and the total value of g is therefore EXACTLY given by:
227	99999*(32+13550/99999) = 3213518 / 99999.
228	
229	The equivalent exact value of g in the metric measure is ("g" in ft/sec^2) * 0.3048
230	Or, g = 9.79490081301 m/s^2.
231	Then,
232	Using the "Solver" function in my TI-85 graphics calculator, and the formula for g that I described in "Part
233	1" of this "Surfer Speed" document, I get the following result for the Equivalent Surf Spot Latitude for my
234	basic formula of Surfer Speed:
235	
236	Exact Latitude = 32.07066048 degrees.
237	
238	Only then, is Max Surfer Speed, mph = 7*SQRT(Hb,ft), EXACTLY.
239	
240	So, if you want to ride a 49-ft wave, you can get up 49 MPH. The Tow-in guys are already doing that, I
241	suppose.
242	
243	But, do you want to ride a 100-foot wave? Your fastest ride might have to be up to 70 MPH. Can you still
244	stand up? You can train by standing on top of a car on the freeway going 70 MPH. Ha!
245	
246	At those high speeds, wind drag would become significant, limiting the top speed achievable by a stand-
247	up surfer. So, it's likely they would not be able to make it across if the Peel Angle is such that they would
248	have to go 70mph to make it.
249	
250	Now,
251	For all you surfers around the world who use the Metric system:
252	
253	25 feet x 0.3048 = 7.62 meters
254	

For Hb = 1 foot, the basic factor in my Surfer Speed formula is 7 MPH, and the equivalent factors used for 255 other measurements of speed are: 256 257 7 MPH x22/15 = 10.2666666666 f/s,10.2666666666 x.3048 = 3.12928 m/s,258 3.12928 x3600 seconds = 11265.408 m/hour, /1000 = 11.265408 Km/hr, 259 11.265408 /1.852 = 6.082833693 Nautical Miles per Hour ("Knots") 260 261 But, we want a formula in metric units that has the basic Breaking Wave Height of 1 Meter, instead of 1 262 263 foot. I meter, in feet, is 1/0.3048 = 3.280839895 ft, so my formulas using MPH and Vfps need to be scaled up 264 by a factor of the SQUARE ROOT of (3.280839895 / 1) = 1.81130889 times. 265 266 267 So, when using MPH, Vsurfer, mph =  $7^{*}$ SQRT(Hb,ft), 268 but now, Hb = 3.280839895 ft. 269 270 Then, Vsurfer,mph = 7\*SQRT(3.280839895) = 12.67916223 MPH 271 272 And, since Vft/s = (22/15) times Vmph, 273 Then, Vft/s = (22/15)\*12.67916223 MPH = 18.5961046 f/s 274 275 276 Since Vm/s = 0.3048 \* Vft/s, Vm/s = 0.3048\*18.5961046 f/s= 5.668092683 m/s 277 278 279 280 So, 281 Our basic Metric Unit formula for Maximum Surfer Speed, in meters per second, is: 282 283 Vsurfer, m/s = 5.668092683 \*SQRT(Hb, m) 284 285 286 In 1 hour, or 3600 seconds, the distance in meters travelled =  $3600^{\circ}$  Vm/s 287 So, Distance, m = 3600\* 5.668092683 m/s = 20,405.13366 meters, or, Distance in Kilometers, = m/1000 = 20.40513366 KM 288 289 290 So, 291 Vsurfer, km/hr = 20.40513366\*SQRT(Hb,m) 292 293 294 The speed in Nautical Miles per Hour, or "Knots", is Vkm/hr / 1.852 295 Or, Vkts = 20.40513366 / 1.852 = 11.01789075 Kts 296 297 So. 298 Vsurfer,kts = 11.01789075\*SQRT(Hb,m) 299 300 \_\_\_\_\_ 301 Let's try some examples: 302 For a 2-meter (true height) breaking wave, how fast could a surfer go on a fast section? 303 Vsurfer,km/hr = 20.40513366\* SQUAREROOT (2) = 28.85721676 Km/hr 304 305

306	So,
307	For a 2-meter wave, Vsurfer, km/hr = 20.40513366*SQRT(2) = 28.85721676
308	
309	For a 3-meter wave, Vsurfer, km/hr = 20.40513366*SQRT(3) = 35.34272823
310	
311	For a 4-meter wave, Vsurfer, km/hr = 20.40513366*SQRT(4) = 40.81026732
312	
313	
314	
315	This concludes Part 2
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317	
318	If you read all of Part 1 and Part 2, Thanks for your patience! I hope somebody tests these results with
319	GPS devices or radar guns. It will be interesting to see just "How Fast CAN a Surfer Go?" in real life.
320	
321	Larry Goddard
322	
323	Submit a Google Moderator question or comment at:
324	http://www.google.com/moderator/#15/e=21f8f&t=21f8f.40
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